# Global Games

David Martinez-Miera

- Diamond and Dybvig exhibit multiple equilibria
  - Very difficult to apply economic recommendations
  - No probabilities and in (general) not dependant on economic fundamentals
  - Quick solution: Sunspot equilibria exogenous probability of each equilibria
- Solution: Global Games
  - Rochet and Vives (2004) and Goldstein and Pauzner (2005)
  - From multiple equilibria to unique equilibria
  - Based on investors signals

- Global games methods to have unique equilibria in bank run setups
  - Rochet and Vives (2004) and Goldstein and Pauzner (2005)
  - Morris and Shin (2003) -currency attacks-
  - Based on Carlsson and Van Damme (1993)
- Model ingredients
  - ullet Each individual receives a private signal of bank returns R
    - Individuals can not put all the signals together (info friction)
  - Such signal is different for each investor  $s_i = R + \varepsilon_i$
  - Where  $\varepsilon_i$  iid error term with distribution  $f(\mu, \sigma)$
  - Each individual's withdrawal decision depends only on her private signal

- Equlibrium
  - Existence of 3 regions in general depends on fundamentals (Return)
  - Fundamental default region banks always default
  - Fundamental safe region banks always survive
  - Coordination problem region withdrawals happen in equlibrium
- Aspects of the equilibrium
  - Threshold strategy equilibria run IFF  $s_i < \bar{S}$
  - Bank withdrawals are function w(R) w'(R) < 0
  - Bank defaults if  $R < \bar{R}$
  - Bank fundamentals drive the run
  - You can have unique equlibria

- Equlibrium
  - Existence of 3 regions in general depends on fundamentals (Return)
  - Fundamental default region banks always default
  - Fundamental safe region banks always survive
  - Coordination problem region withdrawals happen in equlibrium
- Aspects of the equilibrium
  - Threshold strategy equilibria run IFF  $s_i < \bar{S}$
  - Bank withdrawals are function w(R) w'(R) < 0
  - Bank defaults if  $R < \bar{R}$
  - Bank fundamentals drive the run
  - You can have unique equlibria

- Assume two agents with strategic complementarities
- Following payoff structure

$$\begin{array}{ccc} & \textit{NW} & \textit{W} \\ \textit{NW} & (\theta,\theta) & (\textbf{0},\theta-1) \\ \textit{W} & (\theta-1,\textbf{0}) & (\textbf{0},\textbf{0}) \end{array}$$

- With  $1 > \theta > 0$
- Payoff of a given agent doing NW

$$\theta - 1(W_j)$$

- Given strategic complementarities multiple equilibria
- We would want to coordinate on NW no withdrawal

- ullet Let us introduce randomness in heta
- ullet Noone knows heta but each player has a signal

$$s_i = \theta + \varepsilon_i$$

- Where  $\varepsilon_i \sim N(0, \sigma^2)$  and is iid
- Bayesian updating. For simplicity, say the prior of  $\theta$  is "improper prior" or noninformative prior (equally likely over real line)
- Given  $s_i$  the posterior of  $\theta$  is  $N(s_i, \sigma^2)$
- Given  $s_i$  the posterior of  $s_i$  is  $N(s_i, 2\sigma^2)$
- Agent's i conditional payoff

$$E(\theta - 1(W_j)|s_i) = s_i - \Pr(W_j|s_i)$$

- Two different roles played by the signal si
  - First term: si tells me something about fundamental
  - Second term: si tells me something about the distribution of agent j signal sj and thus his strategy

- Lets focus on the second term
- The second term captures the idea of "guessing" each otheris strategy, in a simple but powerful way
- ullet Suppose that everybody follows a cutoff rule with threshold k
  - NW if  $s_i > k$
  - W otherwise
- As  $s_i \sim N(s_i, 2\sigma^2)$  the probabilty of j doing W is

$$\Phi\left(\frac{k-s_i}{\sqrt{2\sigma^2}}\right)$$

So agent i will do NW IFF

$$s_i - \Phi\left(\frac{k - s_i}{\sqrt{2\sigma^2}}\right) > 0$$



- The equlibrium cutoff *k*
- When  $s_i = k$  the agent is indifferent between NW and W

$$k - \Phi\left(\frac{k - k}{\sqrt{2\sigma^2}}\right) = 0 \to k = \frac{1}{2}$$

- So, the unique equilibrium is that every agent invest if his/her signal  $s_i > 1/2$ .
- Intuition:
  - Symmetry: when receiving  $s_i = k$ , the probability of j getting signal  $s_j$  below k is 0.5
  - Strategic uncertainty (guessing each other) implies the second term to be 0.5
  - The first fundamental term have to be 0.5 for equilibrium threshold

David Martinez-Miera () Global Games 9 / 10

- The assumption of threshold strategy can be relaxed
  - Unique equilibrium surviving iterated deletion of strictly dominatedstrategies
- ullet Magically, it does not depends on how noisy the private signal  $\sigma$  is!
- Say  $\sigma \to 0$  so that the game seems to converge to the full information case, the equilibrium is still unique
- Although fundamental uncertainty shrinks, the strategic uncertainty effect remains at 0.5
- As a result, the agent invests only when the fundamental is above 0.5

10 / 10