

## INTEGRAL GEOMETRY SESSION (THU 8/1/26)

ROOM S204 (14-15.50)

**Joonas Ilmavirta** (University of Jyväskylä)

### ***Elastic ray transform (14-14.20)***

Singularities of solutions to the elastic wave equation travel like point particles. Linearization of travel times of elastic waves leads to a ray transform problem. I will describe the linearization (and how it fails to be linear) and the kernel of the ray transform. This is joint work with Antti Kykkänen and Teemu Saksala.

**Miika Sarkkinen** (University of Helsinki)

### ***Non-Abelian light ray transform on stationary Lorentzian manifolds (14.20-14.50)***

In this talk, we consider the invertibility of a non-Abelian light ray transform on Lorentzian manifolds. We show that the transform arises in the problem of recovering a matrix-valued potential on a general globally hyperbolic manifold  $M$  from the knowledge of the source to solution map of a wave equation including a connection 1-form term. Under the assumption that the manifold  $M$  is stationary and that the connection term is time independent, the non-Abelian light ray transform is reduced, by Fourier slicing with respect to time, to a non-Abelian magnetic X-ray transform on the Riemannian base manifold  $N$ . Our main theorem then states that the injectivity of the non-Abelian magnetic X-ray transform on  $N$  is sufficient for the injectivity of the non-Abelian light ray transform on  $M$ .

**Shubham Jathar** (LUT University)

### ***The matrix-weighted real-analytic double fibration transforms (15-15.20)***

In this talk, we present a microlocal result showing that the real-analytic matrix-weighted double fibration transform determines the analytic wavefront set of a vector-valued function. As an application, we prove the injectivity of the matrix-weighted ray transform on two-dimensional, non-trapping, real-analytic Riemannian manifolds with strictly convex boundary. Furthermore, we show that a real-analytic Higgs field can be uniquely recovered from the nonabelian ray transform on real-analytic manifolds of any dimension, provided the manifold has a strictly convex boundary point.

**Eetu Satukangas** (University of Jyväskylä)

### ***One-form tomography in gas giant geometry (15.30-15.50)***

Gas giant geometry is a special type of Riemannian manifold with boundary that describes acoustic wave propagation in gas giant planets. In this talk I will discuss some properties of the geometry and present a new result, based on joint work with Joonas Ilmavirta and Antti Kykkänen, for the solenoidal injectivity of the geodesic ray transform of one-forms in gas giant geometry. The injectivity result answers the following question in integral geometry: Can we uniquely determine a one-form from its integrals over maximal geodesics in gas giant geometry?